

Math 7 Notes

Chapter 2

Find Percents of a Number

Using Mental Math Strategies

Percent of _____
means
↓
Part of "the whole thing"

100% of 1600 = 1600
50% of 1600 = 800
25% of 1600 = 400

Find 10% of a number

THINK

$10\% = \frac{1}{10}$ which means to \div by 10
(move decimal point 1 place left)

Example: 10% of 30 $\overset{\textcircled{3}}{30}$

Find 1% of a number

THINK

$1\% = \frac{1}{100}$ which means to \div by 100
(move decimal point 2 places left)

Example: 1% of 5000 $\overset{\textcircled{50}}{5000}$

Sometimes we can use "unit fractions" to find the percent of a #
↓
Numerator is one

To find $\frac{1}{2}$ of a number, divide by 2

Example
50% of 2400 \div
 $\frac{1}{2}$ of 2400
 $24 \div 2 = 12$ Add 2 zeroes
 $\textcircled{1200}$

To find $\frac{1}{3}$ of a number, divide by 3

$33.\bar{3}\%$ of 270
 $\frac{1}{3}$ of 270
 $27 \div 3 = 9$ Add 1 zero
 $\textcircled{90}$

To find $\frac{1}{4}$ of a number, divide by 4

25% of 36
 $\frac{1}{4}$ of 36
 $36 \div 4 = 9$
 $\textcircled{9}$

To find $\frac{1}{5}$ of a number, divide by 5

Example
20% of 3000
 $\frac{1}{5}$ of 3000
 $3000 \div 5 = 600$ Add 2 zeroes
 $\textcircled{600}$

To find $\frac{1}{6}$ of a number, divide by 6

$16.\bar{6}\%$ of 420
 $\frac{1}{6}$ of 420
 $42 \div 6 = 7$ Add 1 zero
 $\textcircled{70}$

To find $\frac{1}{8}$ of a number, divide by 8

12.5% of 32
 $\frac{1}{8}$ of 32
 $32 \div 8 = 4$
 $\textcircled{4}$

To find $\frac{1}{9}$ of a number, divide by 9

$11.\bar{1}\%$ of 270
 $\frac{1}{9}$ of 270
 $27 \div 9 = 3$ Add 1 zero
 $\textcircled{30}$

For fractions that are NOT unit fractions, to find the percent of a #, we find the unit fraction for that denominator first and then multiply by the numerator.

To find $\frac{2}{3}$ of a number, find $\frac{1}{3}$ of the number and then multiply by 2

Example

$$\begin{aligned} &66.\bar{6}\% \text{ of } 2400 \\ &\frac{2}{3} \\ &\frac{1}{3} \text{ of } 2400 = 800 \\ &800 \times 2 \\ &\quad \mathbf{(1600)} \end{aligned}$$

To find $\frac{3}{4}$ of a number, find $\frac{1}{4}$ of the number and then multiply by 3

$$\begin{aligned} &75\% \text{ of } 280 \\ &\frac{3}{4} \\ &\frac{1}{4} \text{ of } 280 = 70 \\ &70 \times 3 \\ &\quad \mathbf{(210)} \end{aligned}$$

To find $\frac{2}{5}$ of a #, first find $\frac{1}{5}$ and then multiply by 2

Example

$$\begin{aligned} &40\% \text{ of } 35 \\ &\frac{2}{5} \\ &\frac{1}{5} \text{ of } 35 = 7 \\ &7 \times 2 \\ &\quad \mathbf{(14)} \end{aligned}$$

To find $\frac{3}{5}$ of a #, first find $\frac{1}{5}$ and then multiply by 3

$$\begin{aligned} &60\% \text{ of } 250 \\ &\frac{3}{5} \\ &\frac{1}{5} \text{ of } 250 = 50 \\ &50 \times 3 \\ &\quad \mathbf{(150)} \end{aligned}$$

To find $\frac{4}{5}$ of a #, first find $\frac{1}{5}$ and then multiply by 4

$$\begin{aligned} &80\% \text{ of } 40 \\ &\frac{4}{5} \\ &\frac{1}{5} \text{ of } 40 = 8 \\ &8 \times 4 \\ &\quad \mathbf{(32)} \end{aligned}$$

To find $\frac{2}{100}$ of a number, first find $\frac{1}{100}$ and multiply by 2

$$\begin{aligned} &2\% \text{ of } 700 \\ &\frac{2}{100} \\ &\frac{1}{100} \text{ of } 700 \\ &7 \times 2 \\ &\quad \mathbf{(14)} \end{aligned}$$

To find $\frac{3}{100}$ of a number, first find $\frac{1}{100}$ and multiply by 3

$$\begin{aligned} &3\% \text{ of } 6000 \\ &\frac{3}{100} \\ &\frac{1}{100} \text{ of } 6000 = 60 \\ &60 \times 3 \\ &\quad \mathbf{(180)} \end{aligned}$$

Do the same for ↓ 4%, 5%, ...9%

To find $\frac{2}{10}$ of a number, first find $\frac{1}{10}$ and multiply by 2

$$\begin{aligned} &20\% \text{ of } 80 \\ &\frac{2}{10} \\ &\frac{1}{10} \text{ of } 80 = 8 \\ &8 \times 2 \\ &\quad \mathbf{(16)} \end{aligned}$$

To find $\frac{3}{10}$ of a number, first find $\frac{1}{10}$ and multiply by 3

$$\begin{aligned} &30\% \text{ of } 900 \\ &\frac{3}{10} \\ &\frac{1}{10} \text{ of } 900 = 90 \\ &90 \times 3 \\ &\quad \mathbf{(270)} \end{aligned}$$

Do the same for ↓ 40%, 50%, ...90%

Use this strategy for all non-unit fractions we have memorized.

Examples

$$\begin{aligned} &37.5\% \text{ of } 320 \\ &\frac{3}{8} \\ &\frac{1}{8} \text{ of } 320 = 40 \\ &40 \times 3 \\ &\quad \mathbf{(120)} \end{aligned}$$

$$\begin{aligned} &83.\bar{3}\% \text{ of } 180 \\ &\frac{5}{6} \\ &\frac{1}{6} \text{ of } 180 = 30 \\ &30 \times 5 \\ &\quad \mathbf{(150)} \end{aligned}$$

$$\begin{aligned} &77.\bar{7}\% \text{ of } 450 \\ &\frac{7}{9} \\ &\frac{1}{9} \text{ of } 450 = 50 \\ &50 \times 7 \\ &\quad \mathbf{(350)} \end{aligned}$$

$$\begin{aligned} &62.5\% \text{ of } 4800 \\ &\frac{5}{8} \\ &\frac{1}{8} \text{ of } 4800 = 600 \\ &600 \times 5 \\ &\quad \mathbf{(3000)} \end{aligned}$$

Sometimes we find percents of numbers by making combinations of "nice" percents.

- 5% = 10% ÷ 2
- 15% = 10% + 5%
- 150% = 100% + 50%
- 110% = 100% + 10% and many more...
- 300% = 100% × 3
- 99% = 100% - 1%
- 51% = 50% + 1%

Example

Find 15% of 600

$$10\% + 5\%$$

$$10\% \text{ of } 600 + 5\% \text{ of } 600$$

$$\begin{array}{r} 1/10 \qquad 10\% \div 2 \\ 60 + 60 \div 2 \\ 60 + 30 \\ \hline 90 \end{array}$$

You may shorten the steps to something like this.

15% of 600

$$10\% + 5\%$$

$$60 + 30$$

$$\textcircled{90}$$

More Examples...

300% of 5000

$$100\% \times 3$$

$$5000 \times 3$$

$$\textcircled{15,000}$$

51% of 300

$$50\% + 1\%$$

$$150 + 3$$

$$\textcircled{153}$$

5% of 240

$$10\% \div 2$$

$$24 \div 2$$

$$\textcircled{12}$$

125% of 48

$$100\% + 25\%$$

$$48 + 12$$

$$\textcircled{60}$$

250% of 600

$$200\% + 50\%$$

$$1200 + 300$$

$$\textcircled{1500}$$

9% of 2500

$$10\% - 1\%$$

$$250 - 25$$

$$\textcircled{225}$$

11% of 200

$$\begin{array}{r} 10\% + 1\% \\ \frac{10}{100} + \frac{1}{100} \\ 20 + 2 \end{array}$$

$$\textcircled{22}$$

110% of 7000

$$\begin{array}{r} 100\% + 10\% \\ 7000 + 700 \end{array}$$

$$\textcircled{7700}$$

0.5% of 400

$$\begin{array}{r} 1\% \div 2 \\ \frac{1}{100} \div 2 \\ 4 \div 2 \end{array}$$

$$\textcircled{2}$$

49% of 800

$$\begin{array}{r} 50\% - 1\% \\ \frac{50}{100} - \frac{1}{100} \end{array}$$

$$400 - 8$$

$$\textcircled{392}$$

How many different ways can you use mental math to find 40% of 8000

$$\frac{2}{5} \text{ of } 8000$$

$$\begin{array}{r} \frac{1}{5} \text{ of } 8000 = 1600 \\ \times 2 \\ \hline 3200 \end{array}$$

$$\frac{4}{10} \text{ of } 8000$$

$$\begin{array}{r} \frac{1}{10} \text{ of } 8000 = 800 \\ \times 4 \\ \hline 3200 \end{array}$$

$$\begin{array}{r} 50\% - 10\% \\ \frac{50}{100} - \frac{10}{100} \end{array}$$

$$4000 - 800$$

$$3200$$

$$\frac{40}{100} \text{ of } 8000$$

$$\begin{array}{r} \frac{1}{100} \text{ of } 8000 = 80 \\ \times 40 \\ \hline 3200 \end{array}$$