

Math 7 Notes
Lesson 4.1
Terminating and Repeating Decimals

A fraction is a division problem.

Any fraction can be expressed as a decimal by dividing the numerator by the denominator.

$\frac{5}{12} \begin{array}{r} 12 \overline{) 5.0000} \\ \underline{48} \\ 20 \\ \underline{12} \\ 80 \\ \underline{80} \\ 0 \end{array}$	$\frac{1}{3} \begin{array}{r} 3 \overline{) 1.000} \\ \underline{3} \\ 0 \\ \underline{0} \\ 0 \end{array}$
$0.41\overline{6}$	$0.\overline{3}$

Write each of these repeating decimals with correct bar notation.

- $0.\underline{6}36363\dots$ $0.\overline{63}$ $0.2444444\dots$ $0.2\overline{4}$
 $0.15666666\dots$ $0.15\overline{6}$ $0.2454545\dots$ $0.2\overline{45}$

Show the meaning of the bar notation for these decimals.

- $0.\overline{91}$ $\overline{91}9191\dots$ $0.\overline{23}$ $0.2\overline{333}\dots$
 $0.\overline{245}$ $\overline{245}245\dots$ $0.\overline{123}$ $0.1\overline{232323}\dots$

The decimal form of a fraction is either

***terminating** If the remainder eventually becomes zero when you divide, the decimal is terminating.

$\frac{1}{2} = 0.5$

$$\begin{array}{r} 2 \overline{) 1.00} \\ \underline{2} \\ 0 \end{array}$$

***repeating** If the decimal has one or more digits that repeat, it can be written using bar notation.

$\frac{1}{3} = 0.\overline{3}$

To find the decimal for a fraction, without using a calculator, ask yourself these questions:

Memory List

- $\frac{1}{2} = 0.5$ $\frac{1}{5} = 0.2$
 $\frac{1}{3} = 0.\overline{3}$ $\frac{2}{5} = 0.4$
 $\frac{2}{3} = 0.\overline{6}$ $\frac{3}{5} = 0.6$
 $\frac{1}{4} = 0.25$ $\frac{4}{5} = 0.8$
 $\frac{3}{4} = 0.75$

Is it a fraction I have memorized?

$\frac{1}{5} = \frac{2}{10}$

$\frac{1}{6} = 0.1\overline{6}$
 $\frac{2}{6} = \frac{1}{3} = 0.\overline{3}$
 $\frac{3}{6} = \frac{1}{2} = 0.5$
 $\frac{4}{6} = \frac{2}{3} = 0.\overline{6}$
 $\frac{5}{6} = 0.8\overline{3}$

$$\frac{1}{8} + \frac{2}{8} = \frac{3}{8}$$

$$\frac{.125}{.25} = .5$$

$$\frac{.125}{.375} = .333$$

MEMORIZE these
fraction/decimal relationships

$\frac{1}{8} = 0.125$	$\frac{1}{9} = 0.1$	$\frac{1}{10} = 0.1$
$\frac{2}{8} = 0.25$	$\frac{2}{9} = 0.2\bar{2}$	$\frac{2}{10} = 0.2$
$\frac{3}{8} = 0.375$	$\frac{3}{9} = 0.3\bar{3}$	$\frac{3}{10} = 0.3$
$\frac{4}{8} = 0.5$	$\frac{4}{9} = 0.4\bar{4}$	$\frac{4}{10} = 0.4$
$\frac{5}{8} = 0.625$	$\frac{5}{9} = 0.5\bar{5}$	$\frac{5}{10} = 0.5$
$\frac{6}{8} = 0.75$	$\frac{6}{9} = 0.6\bar{6}$	$\frac{6}{10} = 0.6$
$\frac{7}{8} = 0.875$	$\frac{7}{9} = 0.7\bar{7}$	$\frac{7}{10} = 0.7$
	$\frac{8}{9} = 0.8\bar{8}$	$\frac{8}{10} = 0.8$
		$\frac{9}{10} = 0.9$

No Brainer?

Does it have a denominator that is a power of ten (10, 100, 1000...)?

Think...place value as you read the fraction

$\frac{13}{1000}$ "thirteen thousandths" 0.____ = 0.013

$\frac{7}{100}$ "seven hundredths" 0.____ = 0.07

Can you rewrite it as a no brainer?

Can the fraction easily be rewritten with a denominator of 10, 100, 1000, ...?

Think...Rewrite it with a new denominator.

$\frac{7 \times 5}{20 \times 5} = \frac{35}{100} = 0.35$

$\frac{11 \times 4}{25 \times 4} = \frac{44}{100} = 0.44$

Can the fraction be simplified to a fraction I have memorized?

$\frac{22}{44} = \frac{1}{2} = 0.5$

$\frac{18}{16} \div 4 = \frac{3}{4} = 0.75$

$\frac{20}{25} \div 5 = \frac{4}{5} = 0.8$

$\frac{27}{81} \div 27 = \frac{1}{3} = 0.333$

$\frac{5}{25} = \frac{1}{5} = 0.2$

$\frac{24}{30} \div 6 = \frac{4}{5} = 0.8$

Last Resort... Do long division!

numerator / denominator → denominator | numerator

$\frac{3}{16}$

$$\begin{array}{r} 1875 \\ 16 \overline{) 3.000} \\ \underline{-16} \\ 140 \\ \underline{-128} \\ 120 \\ \underline{-112} \\ 80 \end{array}$$

$\frac{7}{11}$

$$\begin{array}{r} 6363 \\ 11 \overline{) 7.000} \\ \underline{-66} \\ 40 \\ \underline{-33} \\ 70 \\ \underline{-66} \\ 40 \end{array}$$

0.1875

0.63

We may need to change mixed numbers or negative numbers to decimals.

Examples:

$$-2\frac{1}{4}$$

$$-2.$$

$$\frac{1}{4} = 0.25$$

$$-2.25$$

$$-\frac{7}{9}$$

$$-0.\bar{7}$$

$$8\frac{3}{20}$$

$$8.$$

$$\frac{3 \times 5}{20 \times 5} = \frac{15}{100}$$

$$8.15$$

Write a fraction that is equivalent to a terminating decimal between two given decimals.

*Extend the decimal places by adding zeros.

*Pick a decimal

*Convert it to a fraction in simplest form

MANY ANSWERS

0.3 and 0.5

$$0.4$$

$$\frac{4}{10} = \frac{2}{5}$$

OR

$$0.30 \quad 0.50$$

$$\frac{31}{100}$$

0.8 and 0.95

$$0.80 \quad 0.95$$

$$\frac{81}{100}$$

0.12 and 0.13

$$.120 \quad 0.130$$

$$\frac{121}{1000}$$

Write decimals as fractions or mixed numbers in simplest form by reading the decimal without saying "point". Read using place value!

-6.2 "Negative six and two tenths"

$$-6\frac{2}{10} = -6\frac{1}{5}$$

Examples:

0.34

$$\frac{34}{100}$$

$$\frac{17}{50}$$

-1.25

$$-1\frac{25}{100}$$

$$-1\frac{1}{4}$$

-0.05

$$-\frac{5}{100}$$

$$-\frac{1}{20}$$

Be precise!

Write Jon's daily practice times as an exact decimal number.

Monday: 1 hour 14 minutes

$$1\frac{14}{60} = 30 \overline{) 7.00} = 7.23\bar{3}$$

$$1\frac{7}{30} = 1.2\bar{3} \text{ hrs}$$

Friday: 2 hours 40 minutes

$$2\frac{40}{60} = 2\frac{2}{3}$$

$$= 2.\bar{6}$$

Tuesday: 45 minutes

$$\frac{45}{100} = \frac{9}{20}$$

$$0.75 \text{ hr}$$

Saturday: 24 minutes

$$\frac{24}{60} = \frac{2}{5}$$

$$\text{or } \frac{2}{5} = 0.4 \text{ hr}$$