

Accelerated MathNotes
Section 5-7
Solving Proportions

A **proportion** is an equation stating that two ratios or rates are equivalent. $\frac{\square}{\square} = \frac{\square}{\square}$

$$\frac{2}{3} = \frac{4}{6}$$

$$\frac{2}{5} = \frac{n}{40}$$

In a proportion the cross products are equal.

$2 \cdot 6 = 12$ $3 \cdot 4 = 12$
 $\frac{2}{3} = \frac{4}{6}$
 $7 \cdot 8 = 56$ $28 \cdot 2 = 56$
 $\frac{7}{28} = \frac{2}{8}$

$$\frac{2}{4} = \frac{x}{4}$$

If crossproduct = 8
 $x = ?$ $x = 2$
 $y = ?$ $y = 4$

Methods to Solve a Proportion

1) Use cross products and solve algebraically.

$$\frac{4.2}{n} = \frac{8}{5}$$

$$4.2(5) = 8 \cdot n$$

$$21 = 8n$$

$$\frac{21}{8} = \frac{8}{8}n$$

$$2.625 = 1n$$

$$2.625 = n$$

Solve using algebraic steps:

$$\frac{3}{17} = \frac{2}{n}$$

$$3 \cdot n = 17 \cdot 2$$

$$3n = 34$$

$$\frac{3n}{3} = \frac{34}{3}$$

$$1n = 11.3\bar{3}$$

$$\text{or } n = 11\frac{1}{3}$$

Round to nearest tenth

$$\frac{n}{19} = \frac{1.8}{7}$$

$$n \cdot 7 = 19(1.8)$$

$$7n = 34.2$$

$$\frac{7n}{7} = \frac{34.2}{7}$$

$$1n = 4.8857 \dots$$

$$n \approx 4.9$$

Methods to Solve a Proportion

2) Use concept of equivalent ratios.

$$\frac{4^{x2}}{5^{x2}} = \frac{8}{n}$$

$n=10$

$$\frac{28 \div 7}{49 \div 7} = \frac{4}{n}$$

$n=7$

Methods to Solve a Proportion

3) Sometimes you can put one of the ratios in simplest form first.

$$\frac{9}{15} = \frac{6}{n}$$

\downarrow

$$\frac{3^R}{5^{x2}} = \frac{6}{n}$$

$n=10$

$$\frac{22}{30} = \frac{55}{n}$$
$$\frac{11^{x5}}{15^{x5}} = \frac{55}{n}$$

$n=75$

Methods to Solve a Proportion

* Use equivalent ratios

* Simplify one of ratios first

* Use cross products

What's the best method to use ?

$$\frac{21}{25} = \frac{8}{n}$$

$$21 \cdot n = 25 \cdot 8$$
$$21n = 200$$

$$\frac{21n}{21} = \frac{200}{21}$$

$$n = 9.523...$$

$n \approx 9.5$

Methods to Solve a Proportion

* Use equivalent ratios

* Simplify one of ratios first

* Use cross products

What's the best method to use ?

$$\frac{12}{18} = \frac{28}{n}$$

$$\frac{2^{x4}}{3^{x4}} = \frac{28}{n}$$

$42 = n$

Methods to Solve a Proportion

- * Use equivalent ratios
- * Simplify one of ratios first
- * Use cross products

$$\frac{11 \times 3}{7 \times 3} = \frac{n}{21}$$

$$n = 33$$

What's the best method to use ?

Carla earns \$74.25 for working 8 hours last week. How much will she earn for working 20 hours?

$\frac{\$}{\text{hour}}$

$$\frac{74.25}{8} = \frac{n}{20}$$

$$74.25(20) = 8n$$

$$1485 = 8n$$

$$\frac{1485}{8} = \frac{8n}{8}$$

$$185.625 = n$$

$\$ 185.63$

The ratio of salt to water in a certain solution is 2 to 17. If the solution contains 34 ounces of salt, how many ounces of water does it contain?

$$\frac{\text{salt}}{\text{water}} \quad \frac{2 \times 17}{17 \times n} = \frac{34}{n}$$

$$n = 289 \text{ oz water}$$

Ted can run 150 meters in 24 seconds. At this rate, how many meters will he run in 38 seconds?

$$\frac{\text{meters}}{\text{sec}} \quad \frac{150}{24} = \frac{n}{38}$$

$$\frac{25}{4} = \frac{n}{38}$$

$$25(38) = 4n$$

$$950 = 4n$$

$$\frac{950}{4} = \frac{4n}{4}$$

$$237.5 = n$$

237.5 m