

Accelerated Math Notes
(Section 8-5)

Solving Equations with Variables on Each Side

Remember:

A solution to an equation is the value for the variable that makes the equation true.

Is $x = -2$ a solution to the equation $6x - 3 = -4x - 23$?

$$6x - 3 = -4x - 23$$

$6(-2) - 3$	$-4(-2) - 23$
$-12 - 3$	$8 - 23$
-15	$8 - 23$
	$-15 \checkmark$

Solve: $7x + 3 = 2x + 23$

$$\begin{array}{r} 7x + 3 = 2x + 23 \\ -2x \quad -2x \\ \hline \end{array}$$

$$\begin{array}{r} 5x + 3 = 23 \\ -3 \quad -3 \\ \hline \end{array}$$

$$5x = 20$$

$$\frac{5x}{5} = \frac{20}{5}$$

$$x = 4$$

Step 1: Choose x term to add or subtract in order to get all x terms on the same side.

Step 2: Simplify.

Step 3: Add or subtract in order to get constants on same side.

Step 4: Simplify.

Step 5: Divide both sides by coefficient of x term.

Check your solution:

$$7x + 3 = 2x + 23$$

$7(4) + 3$	$2(4) + 23$
$28 + 3$	$8 + 23$
31	$31 \checkmark$

Solve another way

$$\begin{array}{r} 7x + 3 = 2x + 23 \\ -7x \quad -7x \\ \hline \end{array}$$

$$3 = -5x + 23$$

$$-20 = -5x$$

$$\frac{-20}{-5} = \frac{-5x}{-5}$$

$$4 = x$$

Solve and check: $-n + 8 = 5n - 7$

$$\begin{array}{r} -n + 8 = 5n - 7 \\ +n \quad +n \\ \hline \end{array}$$

$$8 = 6n - 7$$

$$15 = 6n$$

$$\frac{15}{6} = \frac{6n}{6}$$

$$\frac{5}{2} = n$$

$$\frac{5}{2} = n$$

ck

$$-n + 8 = 5n - 7$$

$-(\frac{5}{2}) + 8$	$5(\frac{5}{2}) - 7$
$-2\frac{1}{2} + 8$	$\frac{25}{2} - \frac{14}{2}$
$5\frac{1}{2}$	$\frac{11}{2} \checkmark$
	$5\frac{1}{2} \checkmark$

Solve and check: $4x + 15 = 2x - 7$

$$\begin{array}{r} 4x + 15 = 2x - 7 \\ -2x \quad -2x \\ \hline 2x + 15 = -7 \\ -15 \quad -15 \\ \hline 2x = -22 \\ \frac{2x}{2} = \frac{-22}{2} \\ x = -11 \end{array}$$

$$\begin{array}{r|l} 4x + 15 = 2x - 7 & \\ 4(-11) + 15 & 2(-11) - 7 \\ -44 + 15 & -22 - 7 \\ -29 & -29 \checkmark \end{array}$$

Solve and check: $2.4 - 3m = 6.4 - 8.8$

$$\begin{array}{r} 2.4 - 3m = 6.4 - 8.8 \\ -2.4 \quad -2.4 \\ \hline -3m = -4.8 \\ \frac{-3m}{-3} = \frac{-4.8}{-3} \\ m = 1.6 \end{array}$$

$$\begin{array}{r} 2.4 - 3m = -2.4 \\ -2.4 \quad -2.4 \\ \hline -3m = -4.8 \\ \frac{-3m}{-3} = \frac{-4.8}{-3} \\ m = 1.6 \end{array}$$

$$\begin{array}{r|l} 2.4 - 3m = 6.4 - 8.8 & \\ 2.4 - 3(1.6) & 6.4 - 8.8 \\ 2.4 - 4.8 & -2.4 \\ 2.4 - 4.8 & -2.4 \\ -2.4 & -2.4 \checkmark \end{array}$$

A car rental agency has two plans. Under Plan A, a car rents for \$80 plus \$20 each day. Under Plan B, a car rents for \$120 plus \$15 a day. What number of days results in the same cost? Write an equation that can be used to solve this problem. Then solve.

Let d = # of days that will result in the same cost

$$\begin{array}{r} \text{cost Plan A} = \text{cost Plan B} \\ 80 + 20d = 120 + 15d \\ -15d \quad -15d \\ \hline 80 + 5d = 120 \\ -80 \quad -80 \\ \hline 5d = 40 \\ \frac{5d}{5} = \frac{40}{5} \\ d = 8 \end{array}$$

8 days

A cell phone provider offers two plans. Under Plan A, the monthly cost is \$20 with a cost of \$0.35 per minute. Under Plan B, the monthly cost is \$35 with a cost of \$0.15 per minute. What number of minutes results in the same cost?

Let m = # of minutes that will result in the same cost

$$\begin{array}{r} \text{Plan A} = \text{Plan B} \\ \text{cost} \quad \text{cost} \\ 20 + 0.35m = 35 + 0.15m \\ -0.15m \quad -0.15m \\ \hline 20 + 0.2m = 35 \\ -20 \quad -20 \\ \hline 0.2m = 15 \\ \frac{0.2m}{0.2} = \frac{15}{0.2} \\ m = 75 \end{array}$$

75 min